

# An Empirical Evaluation of Algorithms for solving Subset Sum Problem in terms of Total Bit Length

# Dissertation

## Submitted To:

Central Department of Computer Science & Information Technology

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Submitted by:

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August, 2015

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# **Student's Declaration**

I hereby declare that I am the only author of this work and that no sources other than the listed here have been used in this work.

Rajendra Shrestha Date: 12 August, 2015



# Tribhuvan University Institute of Science and Technology Central Department of Computer Science and Information Technology

#### Supervisor's Recommendation

I hereby recommend that the dissertation prepared under my supervision by **Mr. Rajendra Shrestha** entitled "**An Empirical Evaluation of Algorithms for solving Subset Sum Problem in terms of Total Bit Length**" be accepted as in fulfilling partial requirement for the completion of Masters Degree of Science in Computer Science & Information Technology.

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## LETTER OF APPROVAL

We certify that we have read this dissertation work and in our opinion it is appreciable for the scope and quality as a dissertation in the partial fulfillment of the requirements of Masters Degree of Science in Computer Science & Information Technology.

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I have done my best to complete this research work. Suggestions from the readers are always welcomed, which will improve this work.

#### Abstract

Subset Sum Problem is an important decision problem in complexity theory and cryptography. Subset sum problem can simply be described as: given a set of positive integers S and a target sum t, is there a subset of S whose sum is t? The complexity of subset sum can be viewed as depending on two parameters: n , the number of values, and m, the precision of the problem (number of bits required to state the problem). Backtracking algorithm for Subset Sum Problem can be modeled as a binary tree where each node represents a single activation of the recursive code. The worst-case time complexity is  $O(2^n)$  when n is used as the complexity parameter [7]. Dynamic Programming breaks a problem down into smaller problems and solves them recursively as divide-and-conquer technique. It solves the problem in  $O(m.n^2)$  time. Dynamic Dynamic Programming is the extension of the Dynamic Programming with a dynamically allocated list of target sums. It has the time complexity of  $2^{O(x)}$  when the total bit length x of the input set is used as the complexity parameter.

The empirical analysis shows that time complexity of DP and DDP increase sub-exponentially when bit length, m, is increased by 1. At the same time BT is not sensitive to m and its time complexity increases exponentially when number of inputs, n, is increased by 1.

**Keywords:** Subset Sum Problem, Backtracking, Dynamic Programming, Dynamic Dynamic Programming, Total Bit Length

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# List of Abbreviations

DDP	-	Dynamic Dynamic Programming
DP	-	Dynamic Programming
SSP	-	Subset Sum Problem
BT	-	Backtracking
	-	ranges (eg 15 ranges from 1 to 5)